### MATHEMATICS STANDARD ARTICULATED BY GRADE LEVEL **Strand 1: Number and Operations** CONCEPT 2008 PO ITEM DESCRIPTION 2003 PO ITEM DESCRIPTION 1. Number Sense Translate between rational numbers 1 Express fractions as ratios, comparing two whole including fractions, decimals, percents, or numbers (e.g., 3/4 is equivalent to 3:4 and 3 to 4). ratios; apply representations of rational Determine the equivalency between and among 4 numbers including fractions, decimals, fractions, decimals, and percents in contextual percents, or ratios. situations. Identify the greatest common factor for two whole 2 Use prime factorization to: 5 determine the greatest common numbers. factor and least common multiples of Determine the least common multiple for two 6 two whole numbers and whole numbers. express a whole number as a product Express a whole number as a product of its prime of its prime factors (including factors, using exponents when appropriate. exponents when appropriate). Demonstrate an understanding of 3 fractions: as a rate or as division of whole numbers. • as parts of wholes or parts of a set, or as locations on a number line.\* Compare two proper fractions, improper fractions, Compare and order positive fractions. 2 decimals, percents, and negative and or mixed numbers. 3 Order three or more proper fractions, improper positive integers. fractions, or mixed numbers. Express or interpret positive and negative 5 numbers from real-life contexts.\* 6 Express the inverse relationships between exponents and roots for perfect squares and cubes.\*

<sup>\*</sup> This performance objective is new to the 2008 Draft Mathematics Standard Articulated by Grade Level.

		Strand 1: Number and	Operations	
CONCEPT	2008 PO	ITEM DESCRIPTION	2003 PO	ITEM DESCRIPTION
2. Numerical Operations	1	Add, subtract, multiply, and divide fractions, decimals, and whole numbers	1	Select the grade-level appropriate operation to solve word problems.
		accurately, efficiently, and flexibly in contextual and non-contextual situations.	2	Solve word problems using grade-level appropriate operations and numbers.
			6	Simplify fractions to lowest terms.
			7	Add or subtract proper fractions and mixed numbers with unlike denominators with regrouping.
			8	Demonstrate the process of multiplication of proper fractions using models.
			9	Multiply proper fractions.
			10	Multiply mixed numbers.
			12	Divide proper fractions.
			13	Divide mixed numbers.
			14	Solve problems involving fractions or decimals (including money) in contextual situations.
	2	Divide multi-digit whole numbers and decimals by decimal divisors accurately, efficiently, and flexibly with and without		
		remainders in contextual and non- contextual situations.*		
	3	Provide a mathematical argument to explain operations with two or more	3	Apply grade-level appropriate properties to assist in computation.
		fractions.	4	Apply the symbols for "" or "—" to represent repeating decimals and ":" to represent ratios, superscripts as exponents.
			5	Use grade-level appropriate mathematical terminology.

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	Strand 1: Number and Operations					
CONCEPT	2008 PO	ITEM DESCRIPTION	2003 PO	ITEM DESCRIPTION		
2. Numerical Operations	4	Apply the commutative, associative, distributive, and identity properties to evaluate numerical expressions involving natural numbers and whole numbers.	15	Simplify numerical expressions using the order of operations with grade-appropriate operations on number sets.		
	5	Simplify numerical expressions (involving fractions, decimals, and exponents) using the order of operations with or without grouping symbols.	15	Simplify numerical expressions using the order of operations with grade-appropriate operations on number sets.		
	M07- S1C2-03	Moved to Grade 7	11	Demonstrate that division is the inverse of multiplication of proper fractions.		
3. Estimation	1	Use benchmarks as meaningful points of comparison for integers and negative fractions in and out of context.*				
	2	Make estimates appropriate to a given situation by	1	Solve grade-level appropriate problems using estimation.		
	<ul> <li>identifying when estimation is appropriate,</li> <li>determining the level of accuracy needed,</li> <li>selecting the appropriate method of estimation, and</li> <li>verifying solutions or determining the reasonableness of situations using various estimation strategies.</li> </ul>	appropriate,	2	Use estimation to verify the reasonableness of a calculation (e.g., Is 5/9 x 3/7 more than 1?).		
		needed,	3	Round to estimate quantities in contextual situations (e.g., round up or round down).		
		estimation, and	4	Estimate and measure for the area and perimeter of polygons using a grid.		
		5	Verify the reasonableness of estimates made from calculator results within a contextual situation.			

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	Strand 2: Data Analysis, Probability, and Discrete Mathematics						
CONCEPT	2008 PO	ITEM DESCRIPTION	2003 PO	ITEM DESCRIPTION			
1. Data Analysis (Statistics)	1	Solve contextual problems by constructing and utilizing a histogram or stem-and-leaf plot with appropriate labels,	2	Construct a histogram, line graph, scatter plot, or stem-and-leaf plot with appropriate labels and title from organized data.			
		title, and intervals from collected data.	8	Solve contextual problems using bar graphs, tally charts, and frequency tables.			
	2	Read, interpret, and answer questions from displays of data.	1	Formulate questions to collect data in contextual situations.			
			3	Interpret simple displays of data including double bar graphs, tally charts, frequency tables, circle graphs, and line graphs.			
			4	Answer questions based on simple displays of data including double bar graphs, tally charts, frequency tables, circle graphs, and line graphs.			
	3	Solve contextual problems by applying the following measures for a data set (extreme values, mean, median, mode, range, and frequency); state how the measures describe the data.	5	Find the mean, median (odd number of data points), mode, range, and extreme values of a given numerical data set.			
	4	Compare data by identifying trends (increasing, decreasing, remaining	6	Identify a trend (variable increasing, decreasing, remaining constant) from displayed data.			
		constant).	7	Compare trends in data related to the same investigation.			

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		Strand 2: Data Analysis, Probability,	and Discret	e watnematics
CONCEPT	2008 PO	ITEM DESCRIPTION	2003 PO	ITEM DESCRIPTION
2. Probability	1	Use data collected from multiple trials of a single event to form a conjecture about the theoretical probability.	3	Predict the outcome of a grade-level appropriate probability experiment.
	2	Determine all possible outcomes (sample space) of a given situation using a	1	Name the possible outcomes for a probability experiment.
		systematic approach (e.g., frequency tables, tree diagrams, charts/tables, ordered pairs, matrices).	4	Record the data from performing a grade-level appropriate probability experiment.
	3	Use theoretical probability to predict experimental outcomes:	3	Predict the outcome of a grade-level appropriate probability experiment.
		<ul> <li>compare the outcome of the experiment to the prediction and</li> <li>replicate the experiment and compare</li> </ul>	5	Compare the outcome of an experiment to predictions made prior to performing the experiment.
		results.	6	Make predictions from the results of student- generated experiments using objects (e.g., coins, spinners, number cubes, cards).
	M05- S2C2-01	Moved to Grade 5	2	Express probabilities of a single event as a decimal.
3. Discrete Mathematics – Systematic Listing and Counting	1	Explore counting problems with Venn diagrams using three attributes.*		
- Comming	2	Build and explore tree diagrams where items repeat (e.g., all possible arrangements of the letters in the word TREE).*		
	M05- S2C3-01	Moved to Grade 5	1	Determine all possible outcomes involving a combination of three sets of three items, using a systematic approach (e.g., 3 different shirts, 3 different pairs of pants, and 3 different belts).
	M05- S2C3-01	Moved to Grade 5	2	Determine all possible arrangements given a set with four or fewer objects using a systematic list, table or tree diagram when order is not important.

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	Strand 2: Data Analysis, Probability, and Discrete Mathematics					
CONCEPT	2008 PO	ITEM DESCRIPTION	2003 PO	ITEM DESCRIPTION		
4. Discrete Mathematics – Vertex-Edge Graphs	1	Analyze a variety of vertex-edge graphs to determine and explain why a particular graph cannot be colored using one fewer color.*				
•	2	Investigate properties of vertex-edge graphs:  • Hamilton path and • Hamilton circuit.*				
	M03- S2C4-02	Moved to Grade 3	1	Find the shortest route on a map from one site to another (vertex-edge graph).		

	Strand 3: Patterns, Algebra, and Functions					
CONCEPT	2008 PO	ITEM DESCRIPTION	2003 PO	ITEM DESCRIPTION		
1. Patterns	1	Describe, analyze, and create sequential patterns using order of operations.	1	Communicate a grade-level appropriate recursive pattern, using symbols or numbers.		
			2	Extend a grade-level appropriate iterative pattern.		
			3	Solve grade-level appropriate iterative pattern problems.		
2. Functions and Relationships	1	Generalize a pattern appearing in a chart, table, or graph using words and expressions.	1	Describe the rule used in a simple grade-level appropriate function (e.g., T-chart, input/output model).		

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	Strand 3: Patterns, Algebra, and Functions					
CONCEPT	2008 PO	ITEM DESCRIPTION	2003 PO	ITEM DESCRIPTION		
3. Algebraic Representations	1	Use algebraic symbols to represent variables in contextual situations.	2	Use variables in contextual situations.		
	2	Evaluate expressions involving the four basic operations by substituting given fractions and decimals for the variable (e.g., $n+3$ , when $n=\frac{1}{2}$ ).	1	Evaluate expressions involving the four basic operations by substituting given fractions for the variable (e.g., $n+3$ , when $n=\frac{1}{2}$ ).		
	3	Solve one-step equations with one variable represented by a letter or symbol, using inverse operations with whole numbers.	5	Solve one-step equations with one variable represented by a letter or symbol, using inverse operations with whole numbers.		
	4	Translate a written phrase in and out of context to an algebraic expression or equation.	3	Translate a written phrase to an algebraic expression (e.g., The quotient of $m$ and 5 is $\frac{m}{5}$ or $m \mid 5$ .).		
			4	Translate a phrase written in context into an algebraic expression (e.g., Write an expression to describe the situation: John has $x$ pieces of candy and buys three more. $x + 3$ ).		
4. Analysis of Change	1	Determine a pattern to predict missing values on a line graph or scatter plot.*				
	M07- S2C1-01	Moved to Grade 7	1	Identify values on a given line graph or scatter plot (e.g., Given a line showing wages earned per hour, what is the wage at five hours?).		

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	Strand 4: Geometry and Measurement					
CONCEPT	2008 PO	ITEM DESCRIPTION	2003 PO	ITEM DESCRIPTION		
1. Geometric Properties	1	Demonstrate the relationship among the diameter, radius, circumference, and definition of a circle and $\pi$ .	8	Identify the diameter, radius, and circumference of a circle or sphere.		
	2	Solve problems with supplementary, complementary, and vertical angles.	7	Identify supplementary or complementary angles.		
	M05- S4C1-01	Moved to Grade 5	1	Classify polygons by their attributes (e.g., number of sides, length of sides, angles, parallelism, perpendicularity).		
	M05- S4C1-02	Moved to Grade 5	2	Draw a geometric figure showing specified properties, such as parallelism and perpendicularity.		
	M07- S4C1-02	Moved to Grade 7	3	Classify prisms, pyramids, cones, and cylinders by base shape and lateral surface shape.		
	M07- S4C1-02	Moved to Grade 7	4	Classify 3-dimensional figures by their attributes.		
	M04- S4C1-03	Moved to Grade 4	5	Compare attributes of 2-dimensional figures with 3-dimensional figures.		
	M05- S4C1-02	Moved to Grade 5	6	Draw triangles with appropriate labels.		
	M03- S4C2-01	Moved to Grade 3	9	Draw a 2-dimensional shape with a given number of lines of symmetry.		

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		Strand 4: Geometry and	Measureme	ent
CONCEPT	2008 PO	ITEM DESCRIPTION	2003 PO	ITEM DESCRIPTION
2. Transformation of Shapes	1	Draw a reflection of a polygon in the coordinate plane using a horizontal or vertical line of reflection (symmetry); explain why the resulting figure is symmetrical.	1	Identify reflections and translations using pictures.
	2	Recognize and identify simple single translations and reflections on a coordinate plane using all four quadrants.	1	Identify reflections and translations using pictures.
	M08- S4C2-03	Moved to Grade 8	2	Perform elementary transformations to create a tessellation.
3. Coordinate Geometry	1	Graph ordered pairs in any quadrant of the coordinate plane.	1	Graph a polygon in the first quadrant using ordered pairs.
	2	State the missing coordinate of a given figure on the coordinate plane using geometric properties to justify the solution.	2	State the missing coordinate of a given figure in the first quadrant of a coordinate grid using geometric properties (e.g., Find the coordinates of the missing vertex of a rectangle when two adjacent sides are drawn.).
4. Measurement	1	Estimate the measure of objects using a scale drawing or map.	11	Determine the actual measure of objects using a scale drawing or map.
	Determine the appropriate unit of measure for a contextual situation and the appropriate tool to measure to the needed precision (including but not	1	Determine the appropriate measure of accuracy within a system for a given contextual situation (e.g., Would you measure the length of your bedroom wall using inches or feet?).	
		limited to length, capacity, angles, time, and mass).	2	Determine the appropriate tool needed to measure to the needed accuracy.
			3	Determine a linear measurement to the appropriate degree of accuracy.
	3	Convert within a single measurement system:  • U.S. customary and • metric.	5	Convert within a single measurement system (U.S. customary or metric) (e.g., How many ounces are equivalent to 2 pounds?).

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		Strand 4: Geometry and	Measureme	ent
CONCEPT	2008 PO	ITEM DESCRIPTION	2003 PO	ITEM DESCRIPTION
4. Measurement	4	Solve problems by determining the	6	Solve problems involving the perimeter of polygons.
		relationship between area and perimeter for regular and irregular	7	Determine the area of triangles.
		polygons.	8	Distinguish between perimeter and area in contextual situation.
	5	Solve problems involving the area of simple polygons using formulas for rectangles and triangles.	9	Solve problems for the areas of parallelograms (includes rectangles).
	6	Describe the relationship between the volume of a figure and the area of its base.*		
	M05- S4C4-02	Moved to Grade 5	4	Measure angles using a protractor.
	M05- S4C4-04	Moved to Grade 7	10	Identify parallelograms having the same perimeter or area.

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		Strand 5: Structure	and Logic	
CONCEPT	2008 PO	ITEM DESCRIPTION	2003 PO	ITEM DESCRIPTION
1. Algorithms and Algorithmic Thinking	1	Analyze algorithms for computing with fractions.	2	Analyze algorithms for computing with decimals.
	2	Create and justify an algorithm to determine the area of a given compound figure using parallelograms and triangles.*		
	M05- S5C1-01	Moved to Grade 5	1	Discriminate necessary information from unnecessary information in a given grade-level appropriate word problem.
2. Logic, Reasoning, Arguments, and Mathematical Proof	1	Develop the problem-solving strategy of working backwards.*		
	2	Solve a non-routine problem by selecting and using a strategy.*		
	3	Solve simple logic problems, including conditional statements, and justify solution methods and reasoning.	1	Solve a simple logic problem from given information (e.g., Which of three different people live in which of three different colored houses?).

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